

Basic Derivatives

$$\frac{d}{dx}(x^{n}) = nx^{n-1}$$
$$\frac{d}{dx}(\sin x) = \cos x$$
$$\frac{d}{dx}(\cos x) = -\sin x$$
$$\frac{d}{dx}(\cos x) = -\sin x$$
$$\frac{d}{dx}(\tan x) = \sec^{2} x$$
$$\frac{d}{dx}(\cot x) = -\csc^{2} x$$
$$\frac{d}{dx}(\cot x) = -\csc^{2} x$$
$$\frac{d}{dx}(\sec x) = \sec x \tan x$$
$$\frac{d}{dx}(\sec x) = -\csc x \cot x$$
$$\frac{d}{dx}(\cos x) = -\csc x \cot x$$
$$\frac{d}{dx}(\ln u) = \frac{1}{u}\frac{du}{dx}$$
$$\frac{d}{dx}(e^{u}) = e^{u}\frac{du}{dx}$$
where u is a function of x, and a is a constant

More Derivatives

 $\frac{d}{dx}\left(\sin^{-1}\frac{u}{a}\right) = \frac{1}{\sqrt{a^2 - u^2}}\frac{du}{dx}$ $\frac{d}{dx}\left(\cos^{-1}x\right) = \frac{-1}{\sqrt{1 - x^2}}$ $\frac{d}{dx}\left(\tan^{-1}\frac{u}{a}\right) = \frac{a}{a^2 + u^2} \cdot \frac{du}{dx}$ $\frac{d}{dx}\left(\cot^{-1}x\right) = \frac{-1}{1 + x^2}$ $\frac{d}{dx}\left(\sec^{-1}\frac{u}{a}\right) = \frac{a}{|u|\sqrt{u^2 - a^2}} \cdot \frac{du}{dx}$ $\frac{d}{dx}\left(\csc^{-1}x\right) = \frac{-1}{|x|\sqrt{x^2 - 1}}$ $\frac{d}{dx}\left(\csc^{-1}x\right) = a^{u(x)}\ln a \cdot \frac{du}{dx}$ $\frac{d}{dx}\left(\log_a x\right) = \frac{1}{x\ln a}$

AP CALCULUS Stuff you MUST know Cold * means topic only on BC **Approx. Methods for Integration Differentiation Rules** Chain Rule Trapezoidal Rule $\frac{d}{dx}[f(u)] = f'(u)\frac{du}{dx} OR \frac{dy}{dx} = \frac{dy}{du}\frac{du}{dx}$ $\int_{a}^{b} f(x)dx = \frac{1}{2} \frac{b-a}{n} [f(x_0) + 2f(x_1) + \dots$ $+2f(x_{n-1})+f(x_n)$] Simpson's Rule **Product Rule** $\frac{d}{dx}(uv) = \frac{du}{dx}v + u\frac{dv}{dx} OR u'v + uv'$ $\int_{a}^{b} f(x) dx =$ $\frac{1}{2}\Delta x[f(x_0) + 4f(x_1) + 2f(x_2) + ...$ $2f(x_{n-2}) + 4f(x_{n-1}) + f(x_n)$ **Ouotient Rule** $\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{\frac{du}{dx}v - u\frac{dv}{dx}}{v^2} \quad OR \frac{u'v - uv'}{v^2}$ **Theorem of the Mean Value** i.e. AVERAGE VALUE If the function f(x) is continuous on [a, b]"PLUS A CONSTANT" and the first derivative exists on the interval (a, b), then there exists a number The Fundamental Theorem of x = c on (a, b) such that Calculus $f(c) = \frac{\int_{a}^{b} f(x) dx}{(b-a)}$ $\int^{b} f(x)dx = F(b) - F(a)$ This value f(c) is the "average value" of where F'(x) = f(x)the function on the interval [a, b]. **Corollary to FTC** Solids of Revolution and friends Disk Method $V = \pi \int_{x=a}^{x=b} \left[R(x) \right]^2 dx$ $\frac{d}{dx}\int_{a(x)}^{b(x)}f(t)dt =$ Washer Method f(b(x))b'(x) - f(a(x))a'(x) $V = \pi \int_{0}^{b} \left(\left[R(x) \right]^{2} - \left[r(x) \right]^{2} \right) dx$ **Intermediate Value Theorem** General volume equation (not rotated) If the function f(x) is continuous on [a, b], $V = \int^{b} Area(x) \, dx$ and y is a number between f(a) and f(b), then there exists at least one number x = c*Arc Length $L = \int_{a}^{b} \sqrt{1 + [f'(x)]^2} dx$ in the open interval (a, b) such that f(c) = y. $=\int_{a}^{b}\sqrt{[x'(t)]^{2}+[y'(t)]^{2}}dt$ **Distance, Velocity, and Acceleration** Mean Value Theorem velocity = $\frac{d}{dt}$ (position) If the function f(x) is continuous on [a, b], acceleration = $\frac{d}{dt}$ (velocity) AND the first derivative exists on the interval (a, b), then there is at least one *velocity vector = $\left\langle \frac{dx}{dt}, \frac{dy}{dt} \right\rangle$ number x = c in (a, b) such that $f'(c) = \frac{f(b) - f(a)}{b - a}.$ speed = $|v| = \sqrt{(x')^2 + (y')^2}$ * displacement = $\int_{0}^{t_f} v dt$ **Rolle's Theorem** distance = $\int_{\text{initial time}}^{\text{final time}} |v| dt$ If the function f(x) is continuous on [a, b]. $\int_{t_0}^{t_f} \sqrt{(x')^2 + (y')^2} dt *$ AND the first derivative exists on the interval (a, b), AND f(a) = f(b), then there average velocity = is at least one number x = c in (a, b) such _ final position – initial position that total time f'(c) = 0. $=\frac{\Delta x}{\Delta t}$

BC TOPICS and important	TRIG identities and v	values
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Values of TrigonometricWates of TrigonometricWates of TrigonometricIntegration of the solution passes through
$$(x_n, y_n)$$
 $(x_n) + f(x_n) + f(x_n) + f(x_n, y_n)$ Values of Trigonometricfor a point curve (D) , the solution passes through (x_n, y_n) $(x_n) + f(x_n, y_{n+1}) + f(x_n, y_{n+1}) + Ax$ Note words: $(x_n) + f(x_n, y_{n+1}) + Ax$ Values of Trigonometric $(x_n) + f(x_n, y_{n+1}) + Ax$ $y(x_n) = y(x_n) + f(x_n, y_{n+1}) + Ax$ $y(x_n) = y(x_n) + f(x_n, y_{n+1}) + Ax$ Note words: $x_{non} + \Delta x$ $x_{non} + \Delta x$ $y_{non} + dx$ $y_{non} = y_{non} + dx$ $y_{non} = y_{non} + dx$ $x_{non} + \Delta x$ $y_{non} = y_{non} + dx$ $x_{non} + \Delta x$ $x_{non} + \Delta x$ $y_{non} = y_{non} + dx$ $x_{non} + \Delta x$ $y_{non} = y_{non} + dx$ $x_{non} + \Delta x$ $y_{non} = y_{non} + dx$ $x_{non} + \Delta x$ $x_{non} + \Delta x$ $y_{non} = y_{non} + dy$ $y_{non} = y_{non} + dy$ $x_{non} + dy$ $x_{non} + dy$ $y_{non} = y_{non} + dy$ $y_{non} = y_{non} + dy$ y_{non}

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